

$$y = \int dy = v_{0y} \int e^{-\frac{c}{m}t} dt - \frac{mg}{c} \int (1 - e^{-\frac{c}{m}t}) dt$$